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Solved Scanner CA Foundation Paper - 3A (New Syllabus)

MULTIPLE CHOICE QUESTIONS AND ANSWERS

2006 - NOVEMBER

[1] Two numbers are in the ratio 2 : 3 and the difference of their squares is 320. The numbers are : (a) 12, 18 (b) 16, 24 (c) 14, 21 (d) None. (1 mark) Answer: (b) Let numbers be 2x and 3x. Therefore, $(3x)^2 - (2x)^2 = 320$ $9x^2 - 4x^2 = 320$ $5x^2 = 320$ $x^2 = 64$ x = 8Numbers are: $2x = 2 \times 8 = 16$ $3x = 3 \times 8 = 24$ [2] If p : q is the sub-duplicate ratio of $p - x^2$: $q - x^2$, then x^2 is : (a) $\frac{p}{p + q}$ (b) $\frac{\mathbf{q}}{\mathbf{p} + \mathbf{q}}$ (C) **<u>qp</u>** (d) None. Answer: (d) As per the given information : $\frac{\mathbf{p}-\mathbf{x}^2}{\mathbf{q}-\mathbf{x}^2} = \frac{\mathbf{P}^2}{\mathbf{q}^2}$ $q^{2} (p - x^{2}) = P^{2}(q - x^{2})$ $pq^{2} - x^{2}q^{2} = p^{2}q - p^{2}x^{2}$ $x^{2} (p^{2} - q^{2}) = pq(p - q)$

[Chapter 🖛 1] Ratio and Proportion, Indices...

3.3

$$X^{2} = \frac{\mathbf{pq} (\mathbf{p}-\mathbf{q})}{\mathbf{p}^{2} - \mathbf{q}^{2}}$$
$$X^{2} = \frac{\mathbf{p} \mathbf{q}}{\mathbf{p}+\mathbf{q}}$$

[3] An alloy is to contain copper and zinc in the ratio 9 : 4. The zinc required to melt with 24 kg of copper is :

(a)
$$10\frac{2}{3}$$
kg (b) $10\frac{1}{3}$ kg
(c) $9\frac{2}{3}$ kg (d) 9kg (1 mark)

Answer:

(a) Let the quantity of copper and zinc in an alloy be 9x kg and 4x kg. Therefore, 9x = 24

$$x = \frac{24}{9} = \frac{8}{3} = 2\frac{2}{3} kg.$$

So zinc = $4x = 4 \times \frac{8}{3} kg.$
= $10\frac{2}{3} kg.$
[4] $7 \log \left(\frac{16}{15}\right) + 5 \log \left(\frac{25}{24}\right) + 3 \log \left(\frac{81}{80}\right)$ is equal to :
(a) 0 (b) 1
(c) $\log 2$ (d) $\log 3$
Answer:
(c) $7 \log \left(\frac{16}{15}\right) + 5 \log \left(\frac{25}{24}\right) + 3 \log \left(\frac{81}{80}\right)$
= $7(\log 16 - \log 15) + 5(\log 25 - \log 24) + 3 \log (\log 81 - \log 80)$
= $7 [4 \log 2 - (\log 3 + \log 5)] + 5 [2 \log 5 - (3 \log 2 + \log 3)]$
 $+ 3 [4 \log 3 - (4 \log 2 + \log 5)]$
= $28 \log 2 - 7 \log 3 - 7 \log 5 + 10 \log 5 - 15 \log 2 - 5 \log 3$
 $+ 12 \log 3 - 12 \log 2 - 3 \log 5 = \log 2$

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2007 - FEBRUARY

- [5] Two numbers are in the ratio 7 : 8. If 3 is added to each of them, their ratio becomes 8 : 9. The numbers are :
 - (a) 14,16 (b) 24,27 (c) 21,24 (d) 16,18 (1 mark) Answer: (c) Let the numbers be 7x and 8x. So, $\frac{7x + 3}{8x + 3} = \frac{8}{9}$ 9 (7x + 3) = 8 (8x + 3) 63x + 27 = 64x + 24 x = 3Numbers are : $7x = 7 \times 3 = 21$

$$8x = 8 \times 3 = 24$$

- [6] A box contains ₹ 56 in the form of coins of one rupee, 50 paise and 25 paise. The number of 50 paise coin is double the number of 25 paise coins and four times the numbers of one rupee coins. The numbers of 50 paise coins in the box is :
 - (a) 64 (b) 32 (c) 16 (d) 14 (1 mark)

Answer:

 (a) Let the number of one – rupee coins be x. Then, number of 50 paise coins is 4x and number of 25 – paise coins is 2x

$$x + \frac{4x}{2} + \frac{2x}{4} = 56$$

4x + 8x + 2x = 56 × 4
14x = 224

$$x = \frac{224}{14} = 16$$

Number of 50 paise coins is $4 \times 16 = 64$

[Chapter 🖛 1] Ratio and Proportion, Indices...

3.5

[7] Value of $(a^{1/8} + a^{-1/8}) (a^{1/8} - a^{-1/8}) (a^{1/4} + a^{-1/4}) (a^{1/2} + a^{-1/2})$ is : (a) a + 1 (b) $a - \frac{1}{a}$ (c) $a^2 + \frac{1}{a^2}$ (d) $a^2 - \frac{1}{a^2}$ (1 mark) Answer: (b) $(a^{1/8} + a^{-1/8}) (a^{1/8} - a^{-1/8}) (a^{1/4} + a^{-1/4}) (a^{1/2} + a^{-1/2})$ = $(a^{1/4} - a^{-1/4}) (a^{1/4} + a^{-1/4}) (a^{1/2} + a^{-1/2})$ $\begin{bmatrix} \text{using } (a^2 - b^2) = (a - b) (a + b) \end{bmatrix}$ = $(a^{1/2} - a^{-1/2}) (a^{1/2} + a^{-1/2})$ = $a^1 - a^{-1}$ = a - **1** [8] The value of the expression : $\mathbf{a}^{\log_{e} b \, \cdot \, \log_{b}^{o} \, \cdot \, \log_{o}^{d} \, \cdot \, \log_{d} t}$ (a) t (b) abcdt (c) (a + b + c + d + t)(d) None. (1 mark) Answer: (a) $a^{\log_{a}^{b} \cdot \log_{b}^{o} \cdot \log_{d}^{d} \cdot \log_{d}^{t}}$ $a \frac{\log^{b}}{\log^{a}} \times \frac{\log^{c}}{\log^{b}} \cdot \frac{\log^{d}}{\log^{c}} \cdot \frac{\log^{f}}{\log^{d}} = \left[using \log a^{b} = \frac{\log^{b}}{\log^{a}} \right]$ $= a \frac{\log^t}{\log^a}$ $= a \log_{a}^{t}$ = t [using **a**^{logom} = m] [9] If $\log_{10000} x = \frac{-1}{4}$, then x is given by: (b) $\frac{1}{10}$ (a) **1**(a) **1**(b) (c) $\frac{1}{20}$ (d) None of these. (1 mark)

Answer:

3.6

(b)
$$\log_{1000} x = -\frac{1}{4}$$

 $(10,000)^{-1/4}$ $x = [using log a^{b} = x, = a^{x} = b]$
 $\frac{1}{(10,000)^{1/4}}$ $= x$
 $= \frac{1}{10} = x$
2007 - MAY

- [10] Eight people are planning to share equally the cost of a rental car. If one person withdraws from the arrangement and the others share equally entire cost of the car, then the share of each of the remaining persons increased by :
 - (a) 1/9 (b) 1/8 (c) 1/7 (d) 7/8 (1 mark)

Answer:

(c) When number of people = 8

then, the share of each person $=\frac{1}{8}$ of the total cost.

When number of people = 7

then, the share of each person $=\frac{1}{7}$ of the total cost

Increase in the share of each person = $\frac{1}{7} - \frac{1}{8} = \frac{1}{56}$ i.e.

 $\frac{1}{7}$ of $\frac{1}{8}$, i.e. $\frac{1}{7}$ of the original share of each person.

- [11] A bag contains ₹ 187 in the form of 1 rupee, 50 paise and 10 paise coins in the ratio 3:4:5. Find the number of each type of coins :
 - (a) 102, 136, 170 (b) 136, 102, 170 (c) 170, 102, 136 (d) None. (1 mark)

Answer:

(a) Let the number of coins be 3x,4x,and 5x. Then, $3x + \frac{4x}{2} + \frac{5x}{10} = 187$ $30x + 20x + 5x = 187 \times 10$ 55x = 1870x = <u>**1870**</u> = 34 Number of coins: One rupee = $3x = 3 \times 34 = 102$ 50 paise = $4x = 4 \times 34 = 136$ 10 paise $=5x = 5 \times 34 = 170$ [12] Simplification of $\frac{\mathbf{x}^{\mathbf{m}+\mathbf{3n}}.\mathbf{x}^{\mathbf{4m}-\mathbf{9n}}}{\mathbf{x}^{\mathbf{6m}-\mathbf{6n}}}$ is : (a) **x**^m (b) **x^{-m}** (d) **x⁻ⁿ** (C) **X**ⁿ (1 mark) Answer: <u>X^{m+3n} . X^{4m-9n}</u> X^{6m-6n} (b) $= \frac{X^{m+3n+4m-9n}}{X^{6m-6n}} \left[using \frac{X^{a}-X^{b}}{X^{a+b}} \right]$ $=\frac{\mathbf{X}^{5\,\mathbf{m}-6\,\mathbf{n}}}{\mathbf{X}^{6\,\mathbf{m}-6\,\mathbf{n}}}$ $= x^{5m-6n-6m+6n} \left[using \frac{x^{a}}{x^{b}} = x^{a-b} \right]$ $= x^{-m}$ [13] If $\log (2a - 3b) = \log a - \log b$, then a = :(a) $\frac{3b^2}{2b-1}$ (b) <u>3b</u> <u>2b-1</u> (C) $\frac{b^2}{2b+1}$ (d) $\frac{3b^2}{2b+1}$ (1 mark)

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.8 Answer: (a) Log (2a - 3b) = log a - log b $\log (2a - 3b) = \log \left(\frac{a}{b}\right)$ $2a - 3b = \frac{a}{b}$ $2ab - 3b^2 = a$ $2ab - a = 3b^2$ $a(2b-1) = 3b^2$ $a = \frac{3b^2}{2b-1}$ 2007 - AUGUST [14] On simplification $\frac{1}{1+z^{a-b}+z^{a-c}} + \frac{1}{1+z^{b-c}+z^{b-a}} + \frac{1}{1+z^{c-a}+z^{c-b}}$ reduces to : (a) $\frac{1}{z^{2(a+b+c)}}$ (b) $\frac{1}{z^{(a+b+c)}}$ (c) 1 (d) 0 (1 mark) Answer: (c) $\frac{1}{1+z^{a-b}+z^{a-c}} + \frac{1}{1+z^{b-c}+z^{b-a}} + \frac{1}{1+z^{c-a}+z^{c-b}}$ $= \frac{1}{1 + \frac{z^{-b}}{z^{-a}} + \frac{z^{-o}}{z^{-a}}} + \frac{1}{1 + \frac{z^{-o}}{z^{-b}} + \frac{z^{-a}}{z^{-b}}} + \frac{1}{1 + \frac{z^{-a}}{z^{-b}} + \frac{z^{-b}}{z^{-o}}}$ $= \frac{Z^{-a}}{Z^{-a} + Z^{-b} + Z^{-c}} + \frac{Z^{-b}}{Z^{-b} + Z^{-a} + Z^{-a}} + \frac{Z^{-c}}{Z^{-c} + Z^{-a} + Z^{-b}}$ $= \frac{Z^{-a} + Z^{-b} + Z^{-c}}{Z^{-a} + Z^{-b} + Z^{-c}}$ = 1

[Chapter = 1] Ratio and Proportion, Indices...

3.9

[15] Ratio of earnings of A and B is 4 : 7. If the earnings of A increase by 50% and those of B decrease by 25%, the new ratio of their earning becomes 8 : 7. What is A's earning ? (a) ₹21,000 (b) ₹26,000 (d) Data inadequate. (c) ₹ 28,000 (1 mark) Answer: (d) Let the earning of A and B be 4x and 7x respectively. New earning of $A = 4x \times 150\% = 6x$ New earning of $B = 7x \times 75\% = 5.25$ Then, $\frac{6x}{5.25x} = \frac{8}{7}$ This does not give the value of x So, the given data is inadequate. [16] P, Q and R are three cities. The ratio of average temperature between P and Q is 11 : 12 and that between P and R is 9 : 8. The ratio between the average temperature of Q and R is : (a) 22 : 27 (b) 27:22 (c) 32:33 (d) None. (1 mark) Answer: (b) $\frac{P}{Q} = \frac{11}{12}$ and $\frac{P}{R} = \frac{9}{8}$ $\frac{P}{Q} = \frac{11 \times 9}{12 \times 9} = \frac{99}{108}$ and $\frac{P}{R} = \frac{9 \times 11}{8 \times 11} = \frac{99}{88}$ Therefore, $\frac{Q}{B} = \frac{108}{88} = \frac{27}{22}$ So, Q : R = 27:22 [17] $\frac{1}{\log_{ab}(abc)} + \frac{1}{\log_{bc}(abc)} + \frac{1}{\log_{aa}(abc)}$ is equal to : (a) 0 (b) 1 (d) - 1 (c) 2 (1 mark)

Answer:

(c)
$$\frac{1}{\log_{ab}^{(abc)}} + \frac{1}{\log_{bc}^{(abc)}} + \frac{1}{\log_{bc}^{(abc)}}$$
$$= \frac{\frac{1}{\log(abc)}}{\log(abc)} + \frac{\frac{1}{\log(abc)}}{\log(abc)} + \frac{\frac{1}{\log(abc)}}{\log(abc)}$$
$$\left[using \ \log_{a} b = \frac{\log b}{\log a} \right]$$
$$= \frac{\log(ab)}{\log(abc)} + \frac{\log(bc)}{\log(abc)} + \frac{\log(ca)}{\log(abc)}$$
$$= \frac{\log (ab \times bc \times ca)}{\log a b c}$$
$$= \frac{\log (ab \times bc \times ca)}{\log(abc)}$$
$$= \frac{\log(abc)^{2}}{\log(abc)} = \frac{2 \log(abc)}{\log(abc)} = 2$$

[18] Number of digits in the numeral for 2^{64} . [Given log 2 = 0.30103] :

(a) 18 digits (b) 19 digits (c) 20 digits (d) 21 digits. (1 mark)

Answer:

(c) 2⁶⁴

= 64 log 2

= 64 × 0.30103

= 19.26592

Number of digit in $2^{64} = 20$.

2007 - NOVEMBER

[19] ₹ 407 are to be divided among A, B and C so that their shares are in the ratio ¹/₄ : ¹/₅ : ¹/₆. The respective shares of A, B, C are :

[Chapter = 1] Ratio and Proportion, Indices... 3.11

(a) ₹ 165, ₹ 132, ₹ 110 (b) ₹ 165, ₹ 110, ₹ 132 (c) ₹ 132, ₹ 110, ₹ 165 (d) ₹ 110, ₹ 132, ₹ 165 (1 mark) Answer: (a) The ratio of share of A, B and C $=\frac{1}{4}:\frac{1}{5}:\frac{1}{6}$ = **<u>15:12:10</u>** = 15:12:10 Therefore, A's share = $407 \times \frac{15}{37} = ₹165$ B's share = 407 × 12/37 = ₹132 C's share = 407 × 10/37 = ₹110 [20] The incomes of A and B are in the ratio 3 : 2 and their expenditures in

- the ratio 5 : 3. If each saves ₹ 1,500, then B's income is :
 - (a) ₹ 6,000 (b) ₹4,500 (c) ₹ 3,000 (d) ₹7,500 (1 mark)

Answer:

(a) Let the income of A and B be 3x and 2x respectively and expenditures of A and B be 5y and 3y respectively.

Therefore, 3x - 5y = 1500 (i) 2x - 3y = 1500 (ii) Solving (i) and (ii) Simultaneously We get x = 3000 and y = 1500

Therefore, B's income = 2x = 2 × 3,000 = ₹ 6,000

[21] If $4^x = 5^y = 20^z$ then z is equal to :

(a) xy (b)
$$\frac{x+y}{xy}$$

(d) **xy x+y** (c) $\frac{1}{XY}$ (1 mark)

(d)
$$4^{x} = 5^{y} = 20^{z} = k \text{ (say)}$$

 $4 = k^{1/x}$
 $5 = k^{1/y}$
 $20 = k^{1/z}$
 $4 \times 5 = 20$
 $k^{1/x} \times k^{1/y} = k^{1/z}$
 $k^{1/x + 1/y} = k^{1/z} \text{ (} x^{m} \times x^{n} = x^{m+n} \text{)}$
 $\frac{x+y}{k^{xy}} = k^{1/z}$
Therefore, $= \frac{x+y}{xy} = \frac{1}{z} \text{ (} x^{m} = x^{n} \text{ m} = n \text{)}$
 $z = \frac{xy}{x+y}$
[22] $\left(\frac{\sqrt{3}}{9}\right)^{5/2} \left(\frac{9}{3\sqrt{3}}\right)^{7/2} \times 9 \text{ is equal to :}$
(a) 1 (b) $\sqrt{3}$
(c) $3\sqrt{3}$ (d) $\frac{3}{9\sqrt{3}}$

(1 mark)

Answer:

(a)
$$\left(\frac{\sqrt{3}}{9}\right)^{\frac{5}{2}} \left(\frac{9}{3\sqrt{3}}\right)^{\frac{7}{2}} \times 9$$

$$= \left(\frac{3^{\frac{1}{2}}}{3^{2}}\right)^{\frac{5}{2}} \left(\frac{3^{2}}{33^{\frac{1}{2}}}\right)^{\frac{7}{2}} \times 3^{2}$$

$$= \left(3^{\frac{1}{2}-2}\right)^{\frac{5}{2}} \left(\frac{3^{2}}{3^{\frac{3}{2}}}\right)^{\frac{7}{2}} \times 3^{2}$$

$$= \left(3^{\frac{-3}{2}}\right)^{\frac{5}{2}} \left(3^{\frac{2-3}{2}}\right)^{\frac{7}{2}} \times 3^{2}$$

[Chapter 🖛 1] Ratio and Proportion, Indices...

3.13

$$= 3^{\frac{-15}{4}} \left(3^{\frac{1}{2}}\right)^{\frac{7}{2}} \times 3^{2}$$

$$= 3^{\frac{-15}{4}} \times 3^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{\frac{-15}{4}} \times 7^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{-\frac{15}{4}} \times 7^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{-\frac{15}{4}} \times 7^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{-2+2} = 3^{0} = 1$$
[23] The value $\frac{\log_{8}8}{\log_{10} \log_{10}4_{10}}$ is :
(a) $3 \log_{10}2$ (b) $7 \log_{10}3$
(c) $3 \log_{e} z$ (d) None. (1 mark)
Answer:
(a) $\frac{\log_{8}^{6}}{\log_{10}^{10} - \log_{10}^{10}}$

$$= \log_{3}^{8} \cdot \log_{10}^{9} \cdot \log_{10}^{4}$$

$$= \log_{3}^{8} \cdot \log_{4}^{2} \cdot \log_{70}^{2}$$

$$= 3\log_{3}^{2} \frac{2}{4} \log_{2}^{8} 2 \log_{10}^{2}$$

$$= 3\log_{3}^{2} \frac{2\log_{2}}{\log_{10}} \cdot \frac{2\log_{2}}{\log_{10}}$$

$$= 3\log_{10}^{2}$$
[2008 - FEBRUARY]

[24] In 40 litres mixture of glycerine and water, the ratio of glycerine and water is 3:1. The quantity of water added in the mixture in order to make this ratio 2:1 is:(a) 45 litres

(a)	15 litres	(b)	10 litres	
(C)	8 litres	(d)	5 litres.	(1 mark)

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Answer:

(d) Quantity of glycerine = $40 \times \frac{3}{4} = 30$ litres

Quantity of water = $40 \times \frac{1}{4} = 10$ litres

Let x liters of water be added to the mixture. Then, total quantity of mixture = (40 + x) litres total quantity of water in the mixture = (10 + x) litres.

So,
$$\frac{30}{10+x} = \frac{2}{1}$$

 $30 = 20 + 2x$
 $2x = 10$
 $x = 5$ litres
Therefore, 5 litres of water must be a

Therefore, 5 litres of water must be added to the mixture.

[25] The third proportional between $(a^2 - b^2)$ and $(a + b)^2$ is :

(a)
$$\frac{\mathbf{a} + \mathbf{b}}{\mathbf{a} - \mathbf{b}}$$
 (b) $\frac{\mathbf{a} - \mathbf{b}}{\mathbf{a} + \mathbf{b}}$
(c) $\frac{(\mathbf{a} - \mathbf{b})^2}{\mathbf{a} + \mathbf{b}}$ (d) $\frac{(\mathbf{a} + \mathbf{b})^3}{\mathbf{a} - \mathbf{b}}$ (1 mark)

Answer:

(d) Let the third proportional be x.

$$\therefore \frac{\mathbf{a^2} - \mathbf{b^2}}{(\mathbf{a} + \mathbf{b})^2} = \frac{(\mathbf{a} + \mathbf{b})^2}{\mathbf{x}}$$

By cross-multiplication
$$x = (\mathbf{a} + \mathbf{b})^2 \frac{(\mathbf{a} + \mathbf{b})^2}{(\mathbf{a^2} - \mathbf{b^2})}$$
$$x = \frac{(\mathbf{a} + \mathbf{b})^3}{(\mathbf{a} - \mathbf{b})}$$

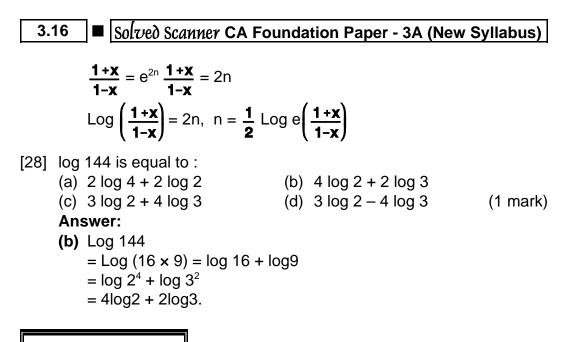
- [26] If $2^{X} 2^{X-1} = 4$ then x^{x} is equal to : (a) 7 (b) 3 (c) 27
 - (d) 9

(1 mark)

[Chapter ➡ 1] Ratio and Proportion, Indices... ■ 3.15

Answer:
(c)
$$2^{x} - 2^{x-1} = 4$$

 $2^{x} - \frac{2^{x}}{2} = 4$
 $2^{x} \left[1 - \frac{1}{2} \right] = 4$
 $2^{x} \left[\frac{1}{2} \right] = 4$
 $2^{x} = 8$
 $2^{x} = 2^{3}$
 $x = 3$
 $x^{x} = 3^{3}$
 $= 27$
[27] If $\mathbf{x} = \frac{\mathbf{0}^{n} - \mathbf{0}^{-n}}{\mathbf{0}^{n} + \mathbf{0}^{-n}}$, then the value of n is:
(a) $\frac{1}{2} \log_{e} \frac{1 + \mathbf{x}}{1 - \mathbf{x}}$ (b) $\log_{e} \frac{1 + \mathbf{x}}{1 - \mathbf{x}}$ (c) $\log_{e} \frac{1 - \mathbf{x}}{1 + \mathbf{x}}$ (d) $\log_{e} \frac{1 - \mathbf{x}}{1 + \mathbf{x}}$ (1 mark)
Answer:
(a) $x = \frac{\mathbf{0}^{n} - \mathbf{0}^{-n}}{\mathbf{0}^{n} + \mathbf{0}^{-n}}$
 $\frac{1}{x} = \frac{\mathbf{0}^{n} + \mathbf{0}^{-n}}{\mathbf{0}^{n} - \mathbf{0}^{-n}}$
Applying Componendo & Dividendo
 $\frac{1 + \mathbf{x}}{1 - \mathbf{x}} = \frac{\mathbf{0}^{n} + \mathbf{0}^{-n} - \mathbf{0}^{n} + \mathbf{0}^{-n}}{2\mathbf{0}^{n}}$



2008 - JUNE

- [29] In what ratio should tea worth ₹ 10 per kg be mixed with tea worth ₹ 14 per kg, so that the average price of the mixture may be ₹ 11 per kg?
 (a) 2:1
 (b) 3:1
 - (a) 2.1 (b) 3.1(c) 3.2 (d) 4.3
 - Answer:
 - (b) Let *x* quantity of tea worth ₹10per kg. be mixed with y quantity worth 14 per kg.

(1 mark)

Total price of the mixture =10x + 14y.

and

Total quantity of the mixture =x + y

Average price of mixture will be $\frac{10x+14y}{x+y} = 11$

10x + 14y = 11x + 11y 3y = x $\frac{\mathbf{x}}{\mathbf{y}} = \frac{\mathbf{3}}{\mathbf{1}}$ or x : y = 3 : 1 which is the required ratio. [Chapter 🍽 1] Ratio and Proportion, Indices...

3.17

[30] The ages of two persons are in the ratio 5:7. Eighteen years ago their ages were in the ratio of 8:13, their present ages (in years) are : (a) 50, 70 (b) 70, 50 (c) 40, 56 (d) None. (1 mark) Answer: (a) Let the present ages of persons be 5x & 7x. Eighteen years ago, their ages = 5x - 18 and 7x - 18. According to given: 5x-18_8 7x-18 13 65x - 234 = 56x - 1449x = 90x = 10Their present ages are $5x = 5 \times 10 = 50$ years $7x = 7 \times 10 = 70$ years. [31] If $x = y^a$, $y = z^b$ and $z = x^c$ then abc is: (a) 2 (b) 1 (c) 3 (1 mark) (d) 4 Answer: **(b)** $Z = x^{c}$ $Z = (y^a)^c (y^a = x)$ $Z = y^{ac}$ $Z = (z^{b})^{ac}(z^{b} = y)$ $Z = Z^{abc}$ $abc = 1(x^{m} = x^{n} then m = n)$ [32] If $\log_2 \left[\log_3 \left(\log_2 x\right)\right] = 1$, then x equals : (a) 128 (b) 256 (1 mark) (c) 512 (d) None. Answer: (c) $\text{Log}_2[\log_3(\log_2 x)] = 1$ $= \log_3(\log_2 x) = 2^1$ (Converting into exponential form) $=\log_2 x = 3^2$ (Converting into exponential form) $= \log_2 x = 9$ $= x = 2^9$ (Converting into exponential form) x = 512.

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.18 2008 - DECEMBER $\left(\frac{\mathbf{a}+\mathbf{b}}{\mathbf{4}}\right) = \frac{1}{2}$ (log a + log b) then: $\frac{\mathbf{a}}{\mathbf{b}} + \frac{\mathbf{b}}{\mathbf{a}}$ [33] If log (a) 12 (b) 14 (d) 8 (c) 16 (1 mark) Answer: (b) Log $\left(\frac{a+b}{4}\right) = \frac{1}{2}$ (Log a + Log b) $\operatorname{Log}\left(\frac{\mathbf{a}+\mathbf{b}}{\mathbf{4}}\right) = \log (ab)^{\frac{1}{2}}$ [Since, $\log_a mn = \log_a m + \log_a n$ and $n \log_a m = \log_a m^n$] Take antilog on both sides. $\frac{\mathbf{a}+\mathbf{b}}{\mathbf{4}}=\sqrt{\mathbf{a}\mathbf{b}}$ a + b = 4 **√ab** Squaring both sides $(a + b)^2 = (4\sqrt{ab})^2$ $a^{2} + b^{2} + 2 ab = 16 ab$ $a^2 + b^2 = 14 ab$ $\frac{\mathbf{a}}{\mathbf{b}} + \frac{\mathbf{b}}{\mathbf{a}} = 14$, which is the required answer

- [34] If A, B and C started a business by investing ₹ 1,26,000, ₹ 84,000 and ₹ 2,10,000. If at the end of the year profit is ₹ 2,42,000 then the share of each is :
 - (a) 72,600, 48,400, 1,21,000 (b) 48,400, 1,21,000, 72,600
 - (c) 72,000, 49,000, 1,21,000 (d) 48,000, 1,21,400, 72,600

(1 mark)

Answer:

- (a) Given : Capital invested by :
 - A : ₹ 126,000, B : ₹ 84,000, C: ₹ 2,10,000 The ratio of their investments is : 126 : 84 : 210 = 3 : 2 : 5

[Chapter ➡ 1] Ratio and Proportion, Indices... ■ 3.19

Profit (at year end) = ₹ 2,42,000 gives
A's Share =
$$\frac{3}{10} \times 2,42,000 = ₹ 72,600$$

B's Share = $\frac{2}{10} \times 2,42,000 = ₹ 48,400$
C's Share = $\frac{5}{10} \times 2,42,000 = ₹ 1,21,000$
[35] If $\frac{P}{q} = -\frac{2}{3}$ then the value of $\frac{2p+q}{2p-q}$ is :
(a) 1 (b) -1/7 (c) 1/7 (d) 7 (1 mark)
Answer:
(c) $\frac{q}{p} = \frac{2}{3}$
So, P = $-\frac{-2q}{3}$ (i)
Now, $\frac{2p+q}{2q-p}$
Substituting the value of p from (i)
 $= \frac{2(-\frac{-2q}{3})+q}{2(-\frac{-2q}{3})-q}$
 $= \frac{-\frac{-4q}{3}+q}{-\frac{-4q}{3}-q}$

3.20 ■ Solved Scanner CA Foundation Paper - 3A (New Syllabus)				
	$= \frac{\frac{-4q+3q}{3}}{\frac{-4q-3q}{3}}$ $= \frac{-q}{3} \times \frac{3}{-7q}$ $= \frac{1}{7}$			
(a) (c)	ourth proportional to x, 2x, (x- a) (x+2) c) (2x+2)	+1) is: (b) (x - (d) (2x		(1 mark)
	nswer: Let the fourth proportional $\frac{x}{2x} = \frac{x+1}{t}$ $\frac{1}{2} = \frac{x+1}{t}$ $t = 2x + 2$ \therefore Fourth proportional to x i.e. x: 2x :: (x + 1) : (2x + 2)			
(a (c	$x = 3^{1/3} + 3^{-1/3}$ then find value a) 3 b) 12	of 3x ³ - 9 (b) 9 (d) 10	9x	(1 mark)
	nswer: a) $x = 3^{1/3} + 3^{-1/3}$ On cubing both sides, we give $x^3 = (3^{1/3} + 3^{-1/3})^3$	get		(1)
	$x^{3} 3 + 3^{-1} + 3 \times 3^{1/3} \times \frac{1}{3}$ $x^{3} = 3 + \frac{1}{3} + 3 (3^{1/3} + 3^{-1/3})$ $x^{3} = 3 + \frac{1}{3} + 3x $ [Using (1))	- 3 ^{-1/3})	
	3	/-		

[Chapter ➡ 1] Ratio and Proportion, Indices...

3.21

$$x^{3} - 3x = \frac{9+1}{3}$$

 $3(x^{3} - 3x) = 10$
 $3x^{3} - 9x = 10$

[38] Find the value of : $[1 - {1 - (1 - x^2)^{-1}}]^{-1/2}$ (a) 1/x (b) x (c) 1 (d) None of these. (1 mark) Answer: **(b)** $[1 - \{1 - (1 - x^2)^{-1}\}^{-1}]^{-1/2}$ $=\left|1-\left\{1-\frac{1}{1-x^{2}}\right\}^{-1}\right|^{-1/2}$ $=\left[1-\left\{\frac{1-x^2-1}{1-x^2}\right\}^{-1}\right]^{-1/2}$ $= \left[1 - \left\{\frac{-x^2}{1 - x^2}\right\}^{-1}\right]^{-1/2}$ $= \left[1 - \left\{\frac{1 - x^2}{x^2}\right\}^{-1}\right]^{-1/2}$ $= \left[1 + \frac{1 - x^2}{x^2}\right]^{-1/2} = \left[\frac{x^2 + 1 - x^2}{x^2}\right]^{-1/2}$ $=\left[\frac{1}{x^2}\right]^{-1/2} = (x^2)^{1/2}$ = X[39] $\log (m + n) = \log m + \log n$, m can be expressed as :

(a) $m = \frac{n}{n-1}$ (b) $m = \frac{n}{n+1}$ (c) $m = \frac{n+1}{n}$ (d) $m = \frac{n+1}{n-1}$ (1 mark)

Answer:

(a) $\log (m + n) = \log m + \log n$ $\log (m + n) = \log (m n)$ [$\log (ab) = \log a + \log b$] Taking Antilog on both side

Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.22 Antilog [log (m + n)] = Antilog [log mn]m + n = mnmn - m = nm(n 1) = n $m = \frac{n}{n-1}$ [40] $\log_4 (x^2 + x) - \log_4 (x+1) = 2$. Find x (a) 16 (b) 0 (c) - 1 (d) None of these. (1 mark) Answer: (a) $\text{Log}_4(x^2 + x) - \text{Log}_4(x + 1) = 2$ $\operatorname{Log}_{4}\left(\frac{\mathbf{x}^{2}+\mathbf{x}}{\mathbf{x}+\mathbf{1}}\right) = 2\left[\operatorname{log}_{a}m - \operatorname{Log}_{a}n = \operatorname{Log}_{a}\left(\frac{\mathbf{m}}{\mathbf{n}}\right)\right]$ $4^2 = \frac{x^2 + x}{x + 1}$ $16 = \frac{x^2 + x}{x + 1}$ $16x + 16 = x^2 + x$ $x^2 - 15x - 16 = 0$ $x^2 - 16x + x - 16 = 0$ x(x-16) + 1(x-16) = 0(x + 1) (x - 16) = 0x = -1 or x = 16Since x = -1 is not possible therefore x = 16

[41] 2ⁿ + 2^{n−1} 2 ⁿ⁺¹ □2 ⁿ		
(a) 1/2	(b) 3/2	
(c) 2/3	(d) 1/3	(1 mark)

2009 - DECEMBER

[Chapter 🍽 1] Ratio and Proportion, Indices...

3.23

Answer: (b) $\frac{2^{n}+2^{n-1}}{2^{n+1}-2^{n}}$ $= 2^{n} (1 + \frac{1}{2})$ = 2n (2 – 1) = $\frac{3}{2}=\frac{3}{2}$ [42] If $2^x \times 3^y \times 5^z = 360$ Then what is the value of x, y, z.? (b) 1, 2, 3 (a) 3, 2, 1 (c) 2, 3, 1 (d) 1, 3, 2 (1 mark) Answer: (a) $2^x \times 3^y \times 5^z = 360$(1) The factors of 360 are: $2^3 \times 3^2 \times 5$. $2^3 \times 3^2 \times 5^1 = 360....(2)$ On comparing (1) and (2), we get; x = 3, y = 2 and z = 1[43] Find the value of $\log_{10}\sqrt{25} \, \log_{10} (2^3) + \log_{10} (4)^2 \, k^2$ (b) 10 (a) x (d) None. (c) 1 (1 mark) Answer: (c) $[\log_{10} \sqrt{25} - \log_{10}(2^3) + \log_{10}(4^2)]^x$ $= [\log_{10} 5 - 3 \log_{10} 2 + \log_{10} (2^4)]^x$ $= [\log_{10} 5 - 3 \log_{10} 2 + 4 \log_{10}^{2}]^{x}$ $= [\log_{10} 5 + \log_{10}^{2}]^{\times}$ = $[\log_{10} (5 \times 2)]^{x} [\log (mn) = \log m + \log n]$ $= [\log_{10} 10]^{x}$ $= 1^{x} [\log_{a} a = 1]$ = 1

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus)

2010 - JUNE

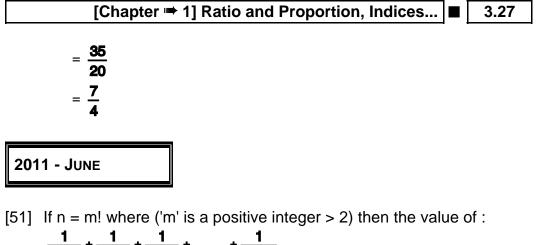
[44] If $\log_a b + \log_a c = 0$ then (b) b = -c(a) b = c(d) b and c are reciprocals. (1 mark) (c) b = c = 1Answer: (d) $\log_a b + \log_a c = 0$ $\log_{\mathbf{p}} \mathbf{bc} = 0$ $a^0 = bc$ bc = 1∴ b = **1**/**c** So, b and c are reciprocals. [45] What must be added to each term of the ratio 49 : 68, so that it becomes 3:4? (a) 3 (b) 5 (c) 8 (d) 9 (1 mark) Answer: (c) Let the number added be x <u>49 + x _ 3</u> 68 + x 4 196 + 4x = 204 + 3xx = 8[46] The students of two classes are in the ratio 5:7, if 10 students left from each class, the remaining students are in the ratio of 4 : 6 then the number of students in each class is: (a) 30, 40 (b) 25, 24 (c) 40, 60 (d) 50,70 (1 mark) Answer:

- (c) Let the ratio be 5x : 7x
 - If 10 student left, Ratio became 4 : 6

[Chapter 🍽 1] Ratio and Proportion, Indices...

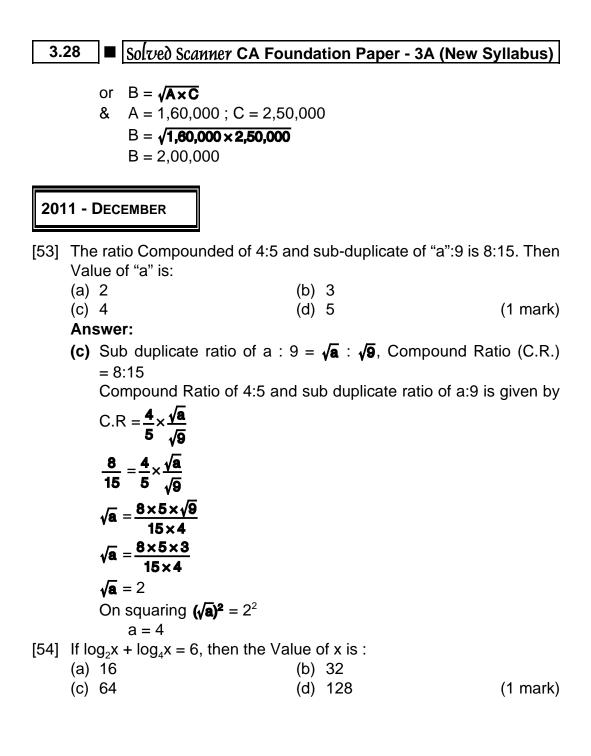
3.25

 $\frac{5x-10}{7x-10} = \frac{4}{6}$ 30x - 60 = 28x - 402x = 20x = 10No. of students in each class is 5x and 7x ÷ i.e. 50, 70 2010 - DECEMBER [47] The value of $2 \log x + 2 \log x^2 + 2 \log x^3 + \dots +$ $2 \log x^n$ will be : (a) <u>**n(n + 1)logx**</u> 2 (b) n(n+1) log x (c) $n^2 \log x$ (d) None of these. (1 mark) Answer: **(b)** $2 \log x + 2 \log x^2 + 2 \log x^3 + \dots$ $2[\log x + \log x^2 + \log x^3 + \dots]$ $2[\log x + 2\log x + 3\log x +]$ 2log x[1 + 2 + 3 n] 2 log x × <u>n(n +1)</u> 2 $= n(n + 1) \log x$ [48] The recurring decimal 2.7777...... can be expressed as: (a) 24/9 (b) 22/9 (c) 26/9 (d) 25/9 (1 mark) Answer: (d) 2.7777 2 + 0.7 + 0.07 + 0.007 + $2 + \left(\frac{7}{10} + \frac{7}{100} + \frac{7}{1000} + \dots\right)$



[52] In a film shooting, A and B received money in a certain ratio and B and C also received the money in the same ratio. If A gets ₹ 1,60,000 and C gets ₹ 2,50,000. Find the amount received by B ?

(a) ₹2,00,000	(b) ₹2,50,000	
(c) ₹1,00,000	(d) ₹1,50,000	(1 mark)
Answer:		
(a) Given : A : B = B : C		
$B^2 = A \times C$		



Answer:

- (a) If $\log_2 x + \log_4 x = 6$ $\frac{\log x}{\log 2} + \frac{\log x}{\log 4} = 6$ $\frac{\log x}{\log 2} + \frac{\log x}{\log 2^2} = 6$ $\frac{\log x}{\log 2} + \frac{\log x}{2\log 2} = 6$ $\frac{\log x}{\log 2} \left[1 + \frac{1}{2}\right] = 6$ $\frac{\log x}{\log 2} \times \frac{3}{2} = 6$ $\frac{\log x}{\log 2} = 6 \times \frac{2}{3}$ $\frac{\log x}{\log 2} = 4$ $\log x = 4 \log 2$ $\log x = \log 2^4$ $x = 2^4$ x = 16
- [55] If X Varies inversely as square of Y and given that Y = 2 for X = 1, then the Value of X for Y = 6 will be:
 - (a) 3 (b) 9 (c) 1/3 (d) 1/9 (1 mark) Answer:
 - (d) Given x varies inversely as square of y

i. e. x
$$\frac{1}{y^2}$$

x = k $\frac{1}{y^2}$
x = $\frac{k}{y^2}$(1)
Given x = 1, y = 2 then

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.30 $1 = \frac{\mathbf{k}}{(2)^2}$ $\mathbf{k} = 1 \times 4 = 4$ Now putting $y = 6_1 k = 4$ in equation (1) $X = \frac{4}{6^2}$ $X = \frac{4}{36} = \frac{1}{9}$ 2012 - JUNE [56] The value of $\frac{(3^{n+1} + 3^n)}{(3^{n+3} - 3^{n+1})}$ is equal to: (a) 1/5 (b) 1/6 (c) 1/4 (d) 1/9 (1 mark) Answer: (b) $\frac{3^{n+1}+3^n}{3^{n+3}-3^{n+1}} = \frac{3^n \cdot 3^1 + 3^n}{3^n \cdot 3^3 - 3^n \cdot 3^1}$ $=\frac{3^n (3^1+1)}{3^n (3^3-3)}$ $=\frac{(3+1)}{(27-3)}$ $=\frac{4}{24}$ = <mark>1</mark> 6 [57] If logx y = 100 and $log_2 x = 10$, then the value of 'y' is : (b) 2¹⁰⁰ (a) 2¹⁰ (d) 2^{10,000} (c) $2^{1,000}$ (1 mark) Answer: (c) Given $\log_x y = 100$ (1) $\log_2 x = 10....(2)$ Multiply eq (1) & (2) $\log_x y \cdot \log_2 x = 100 \times 10$

[Chapter 🍽 1] Ratio and Proportion, Indices...

3.31

 $\frac{\log y}{\log x} \times \frac{\log x}{\log 2} = 1,000$ $\log y = 1,000 \log 2$ $\log y = \log 2^{1,000}$ $y = 2^{1,000}$ [58] Which of the numbers are not in proportion? (b) 7, 14, 6 (a) 6, 8, 5, 7 (c) 18, 27, 12, 18 (d) 8, 6, 12, 9 (1 mark) Answer: (a) If say a, b, c, d are in proportion they bear a common ratio that is $\frac{\mathbf{a}}{\mathbf{b}} = \frac{\mathbf{c}}{\mathbf{d}}$ Option (A) $\frac{6}{8}$ $\frac{5}{7}$ Option (B) $\frac{7}{3} = \frac{14}{6}$ Option (C) $\frac{18}{27} = \frac{12}{18}$ Option (D) $\frac{8}{6} = \frac{12}{9}$ 2012 - DECEMBER [59] Find the value of x, if $x (x)^{\frac{1}{3}} = (x^{\frac{1}{3}})^{x}$ (a) 3 (b) 4 (c) 2 (d) 6 (1 mark) Answer: **(b)** If $x^1 (x)^{1/3} = (x^{1/3})^x$ $x^{1+1/3} = x^{\frac{1}{3}x}$ $X^{4/3} = \mathbf{x}^{\frac{1}{3}\mathbf{x}}$

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus)

on comparing 43x = 12 x = 4

[60] Which of the following is true.

 $|f\frac{1}{ab} + \frac{1}{bc} + \frac{1}{ca} = \frac{1}{abc}$ (b) $\log\left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right) = abc$ (a) $\log(ab + bc + ca) = abc$ (c) $\log(abc) = 0$ (d) $\log (a + b + c) = 0$ (1 mark) Answer: (d) Given $\frac{1}{ab} + \frac{1}{bc} + \frac{1}{ca} = \frac{1}{abc}$ $\frac{\mathbf{c} + \mathbf{a} + \mathbf{b}}{\mathbf{abc}} = \frac{1}{\mathbf{abc}}$ a + b + c = 1taking log on both side $\log (a + b + c) = \log 1$ $\log (a + b + c) = 0$ [61] Find two numbers such that mean proportional between them is 18 and third proportional between them is 144 (a) 9,36 (b) 8, 32 (c) 7,28 (d) 6,24 (1 mark) Answer: (a) Let two Nos. be x and y Mean proportion between x and y is 18 So, x, 18, y are in proportion x:18::18:y $\frac{\mathbf{x}}{\mathbf{18}} = \frac{\mathbf{18}}{\mathbf{y}}$ xy = 324

2013 - JUNE

[62] For what value of x, the equation $(\log_{\sqrt{x}} 2)^2 = \log_x^2$ is true? (a) 16 (b) 32 (c) 8 (d) 4 (1 mark) Answer: (a) Given $(\log_{\sqrt{x}})^2 = \log_x 2$ $\left(\frac{\log 2}{\log \sqrt{x}}\right)^2 = \left(\frac{\log 2}{\log x}\right)$

3.34 ■ Solved Scanner CA Foundation Paper - 3A (New Syllabus)				
$(\frac{\log 2}{\log x^{1/2}})^2 = \frac{\log 2}{\log x}$ $\left(\frac{\log 2}{\frac{1}{2}\log x}\right)^2 = \frac{\log 2}{\log x}$ $\left(\frac{2\log 2}{\frac{1}{2}\log x}\right)^2 = \left(\frac{\log 2}{\log x}\right)$ $4\left(\frac{\log 2}{\log x}\right)^2 = \left(\frac{\log 2}{\log x}\right)^1$ $4\frac{\log 2}{\log x} = 1$ $4\log 2 = \log x$ $\log 2^4 = \log x$ $2^4 = x x = 16$				
[63]	The mean proportional between (a) 33 (c) 35 Answer: (d) Mean Proportion = $\sqrt{24 \times 5}$	(b) 34 (d) 36	(1 mark)	
[64]	$=\sqrt{1296}$ = 36 The triplicate ratio of 4 : 5 is: (a) 125 : 64 (c) 64 : 125 Answer: (c) The triplicate Ratio of 4 : 5	(b) $16:25$ (d) $120:46$ $5 = 4^3:5^3$ = $64:125$	(1 mark)	

2013 - DECEMBER

[65] If $\sqrt[3]{a} + \sqrt[3]{b} + \sqrt[3]{c}$ then the value of $\left(\frac{a+b+c}{3}\right)^3$ (a) abc (b) 9abc (c) $\frac{1}{abc}$ (d) $\frac{1}{9abc}$ (1 mark) Answer: (a) If $3\sqrt{a} + 3\sqrt{b} + 3\sqrt{c} = 0$ $a^{1/3} + b^{1/3} + c^{1/3} = 0$ $a^{1/3} + b^{1/3} = -c^{1/3}$ (i) Cube on both side $(a^{1/3} + b^{1/3})^3 = (-c^{1/3})^3$ $(a^{1/3})^3 + (b^{1/3})^3 + 3 \cdot a^{1/3} \cdot b^{1/3} (a^{1/3} + b^{1/3}) = c$ $a + b + 3a^{1/3}$. $b^{1/3}$. $(-c^{1/3}) = c$ $a + b - c 3a^{1/3}$. $b^{1/3}$. $c^{1/3} = c$ $a + b + c = 3a^{1/3}$. $b^{1/3}$. $c^{1/3}$ $\left(\frac{a+b+c}{3}\right) = \frac{3a^{1/3}.b^{1/3}.c^{1/3}}{3}$ $\left(\frac{\mathbf{a}+\mathbf{b}+\mathbf{c}}{\mathbf{3}}\right)^{\mathbf{3}} = (a^{1/3}. b^{1/3}. c^{1/3})^{3} = abc$ [66] Find three numbers in the ratio 1 : 2 : 3, so that the sum of their

squares is equal to 504 (a) 6, 12, 18 (b) 3, 6, 9 (d) 5, 10, 15 (c) 4, 8, 12 (1 mark) Answer: (a) Since Ratio of three Number is 1:2:3 First No. = X Second No. = 2xThird No. = 3x Sum of squares of numbers = 504 $(x)^{2} + (2x)^{2} + (3x)^{2} = 504$ $x^{2} + 4x^{2} + 9x^{2} = 504$

Solved Scanner CA Foundation Paper - 3A (New Syllabus)

$$14x^{2} = 504$$

$$x^{2} = \frac{504}{14}$$

$$x^{2} = 36$$

$$x = 6$$
First No. = x = 6
Second No. = 2x = 2 × 6 = 12
Third No. = 3x = 3 × 6 = 18
[67] The value of log₄ 9 . log₃ 2 is:
(a) 3 (b) 9
(c) 2 (d) 1 (1 mark)
Answer:
(d) log₄9 . log₃2

$$= \frac{log{9}}{log{2}} \cdot \frac{log{2}}{log{3}}$$

$$= \frac{log{9}}{log{2}} \cdot \frac{log{2}}{log{3}}$$

$$= 1$$
[68] The value of (log_y x . log_z y . log_x z)³ is
(a) 0 (b) - 1
(c) 1 (d) 3 (1 mark)
Answer:
(c) (log_y x . log_z y . log_z z)³

$$= \left(\frac{logx}{logy} \cdot \frac{logz}{logz}\right)^{3}$$

$$= (1)^{3}$$

$$= 1$$
[69] Divide 80 into two parts so that their product is maximum, then the

numbers are: (a) 25 55 (b) 35 45

(a)	23, 33	(U)	55, 45	
(C)	40, 40	(d)	15, 65	(1 mark)

3.37

Answer:

(c) The sum of two No. = 80First No. = xSecond No. = (80 - x)Product two No = x. (80 - x) $P = 80x - x^2$ (1) w.r.f. (x) $\frac{dp}{dx} = 80 - 2x$ $\frac{d^2p}{dx^2} = -2$(3) For max/minima **<u>dp</u>** = 0 dx 80 - 2x = 02x = 80x = 40x = 40 in equation (iii) $\frac{d^2p}{dx^2} = -2$ (Negative) function is maximum at x = 40Numbers are 40, (80 40) = 40, 40

2014 - JUNE

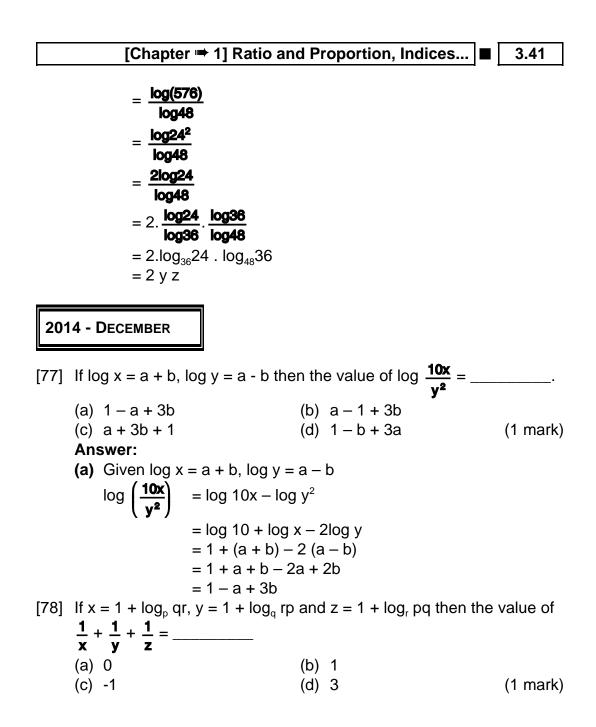
[70] If x : y = 2:3, then (5x+2y):(3x-y) =_____ (a) 19:3 (b) 16:3 (c) 7:2 (d) 7:3 (1 mark) Answer: (b) Given, x : y = 2:3

Let
$$x = 2k, y = 3k$$

 $(5x + 2y) : (3x - y)$
 $= \frac{(5x + 2y)}{(3x - y)}$
 $= \frac{5 \times 2k + 2 \times 3k}{5 \times 2k - 3k}$
 $= \frac{10k + 6k}{6k - 3k}$
 $= 16 : 3$
[71] If $(25)^{150} = (25x)^{50}$; then the value of x will be :
(a) 5^3 (b) 5^4
(c) 5^2 (d) 5 (1 mark)
Answer:
(b) If $(25)^{150} = (25x)^{50}$
 $25^{150} = 25^{50} \times 5^{50}$
 $\frac{25^{150}}{25^{50}} = x^{50}$
 $25^{100} = x^{50}$
 $(5^2)^{100} = x^{50}$
 $5^4 = x$
 $x = 5^4$
[72] The value of $(\frac{y^k}{y^b})^{a^2 + bb + b^2} \times (\frac{y^b}{y^o})^{b^2 + bb + o^2} \times (\frac{y^e}{y^e})^{a^2 + ac + a^2}$
(a) y (b) -1
(c) 1 (d) None of these (1 mark)
Answer:
(c) $(\frac{y^k}{y^b})^{a^2 + ab + b^2} (\frac{y^b}{y^o})^{b^2 + b + o^2} \cdot (\frac{y^o}{y^a})^{a^2 + ac + a^2}$

[Chapter ➡ 1] Ratio and Proportion, Indices... 3.39 $= (y^{a-b})^{a^2 + ab + b^2} \cdot (y^{b-c})^{b^2 + bc + c^2} \cdot (y^{c-a})^{c^2 + ac + a^2}$ $= y^{a^3-b^3} \cdot y^{b^3-c^3} \cdot y^{c^3-a^3}$ $= y^{a^3-b^3+b^3-c^3+c^3-a^3}$ $= y^0 = 1$ [73] If the salary of P is 25% lower than that of Q and the salary of R is 20% higher than that of Q, the ratio of the salary of R and P will be: (a) 5:8 (b) 8:5 (c) 5:3 (d) 3:5 (1 mark) Answer: (b) Let Salary of Q= 100 Salary of P = 100 - 25% of 100 = 100 - 25= 75Salary of R = 100 + 20% of 100 = 100 + 20= 120Ratio of salary of R and P = 120:75 = 8:5[74] If $x^2+y^2=7xy$, then log $\frac{1}{3}(x+y) =$ ____. (b) $\frac{1}{2} (\log x + \log y)$ (a) $(\log x + \log y)$ (d) $\frac{1}{3}$ (log x + log y) (c) $\frac{1}{3}$ (log x / log y) (1 mark) Answer: **(b)** If $x^2 + y^2 = 7xy$ $x^{2} + y^{2} + 2xy = 7xy + 2xy$ $(x + y)^2 = 9xy$ taking log on both side $\log (x + y)^2 = \log 9xy$ $2 \log (x + y) = \log 9 + \log x + \log y$ $2 \log (x + y) = \log 3^2 + \log x + \log y$ $2 \log (x + y) = 2 \log 3 + \log x + \log y$ $2 \log (x + y)$ $2 \log 3 = \log x + \log y$

Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.40 $2\left[\log \frac{(\mathbf{x}+\mathbf{y})}{\mathbf{3}}\right]$ $= \log x + \log y$ $\log \frac{(x+y)}{3} = \frac{1}{2} [\log x + \log y]$ [75] A person has assets worth ₹ 1,48,200. He wish to divide it amongst his wife, son and daughter in the ratio 3:2:1 respectively. From this assets, the share of his son will be: (a) ₹24,700 (b) ₹ 49,400 (c) ₹74,100 (d) ₹ 37,050 (1 mark) Answer: (b) A person has Assets worth = ₹ 1,48,200 Ratio of share of wife, son & daughter = 3:2:1Sum of Ratio = 3 + 2 + 1 = 6Share of Son = $\frac{2}{6} \times 1,48,200$ = 49,400 [76] If $x = \log_{24} 12$, $y = \log_{36} 24$ and $z = \log_{48} 36$, then xyz + 1 =____ (a) 2xy (b) 2xz (c) 2yz (d) 2 (1 mark) Answer: (c) If $x = \log_{24}12$, $y = \log_{36}24$ and $z = \log_{48}36$ then XYZ + 1 $= \log_{24} 12 \times \log_{36} 24 \times \log_{48} 36 + 1$ $= \frac{\log 12}{\log 24} \cdot \frac{\log 24}{\log 36} \cdot \frac{\log 36}{\log 48} + 1$ = **log12** + 1 log48 _ <u>log12 + log</u>48 log48 _ <u>log(12 × 48)</u> log48



Solved Scanner CA Foundation Paper - 3A (New Syllabus)

Answer: (h) If \

(b) If
$$x = 1 + \log_p qr$$
, $y = 1 + \log_q rp$, $z = 1 + \log_r pq$
 $x = 1 + \frac{\log qr}{\log p}$
 $x = \frac{\log p + \log qr}{\log p}$
 $x = \frac{\log pqr}{\log p}$
 $\frac{1}{x} = \frac{\log p}{\log pqr}$
Similarly
 $\frac{1}{y} = \frac{\log q}{\log pqr}$
 $\frac{1}{z} = \frac{\log q}{\log pqr}$
 $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \frac{\log p}{\log pqr} + \frac{\log q}{\log pqr} + \frac{\log r}{\log pqr}$
 $= \frac{\log p + \log q + \log r}{\log pqr}$
 $= \frac{\log p + \log q + \log r}{\log pqr}$
 $= 1$

[79] For three months, the salary of a person are in the ratio 2 : 4 : 5. If the difference between the product of salaries of the first two months and last two months is ₹ 4,80,00,000; then the salary of the person for the second month will be:

₹ 4,000	(b) ₹6,000				
₹ 8,000	(d) ₹12,000	(1 mark)			
swer:					
(c) Ratio of the salary of a person in three months = 2 : 4 : 5					
_et,	Salary of I^{st} month = 2x				
	Salary of II nd month = $4x$				
	Salary of III^{rd} month = 5x				
	₹ 4,000 ₹ 8,000 swer: Ratio of the sa _et,	₹ 8,000 (d) ₹ 12,000 swer: Ratio of the salary of a person in three months = 2 : 4 Let, Salary of I st month = $2x$ Salary of II nd month = $4x$			

Given

(Salary of Product of last two months) – (Salary of Product Ist two months)

3.43

= 4,80,00,000 (4x.5x) - (2x.4x) = 4,80,00,000 $20x^{2} \quad 8x^{2} = 4,80,00,000$ $12x^{2} = 4,80,00,000$ $x^{2} = 40,00,000$ x = 2,000

Salary of the person for second month = $4x = 4 \times 2,000 = 8,000$

2015 - JUNE

- [80] A dealer mixes rice costing ₹ 13.84 per Kg. with rice costing ₹ 15.54 and sells the mixture at ₹ 17.60 per Kg. So, he earns a profit of 14.6% on his sale price. The proportion in which he mixes the two qualities of rice is:
 - (a) 3:7 (b) 5:7 (c) 7:9 (d) 9:11 (1 mark) Answer: (a) Let SP of mixture is ₹ 100 Then Profit = 14.6% of 100 = 14.6 CP of mixture = (100 - 14.6)= 85.4If SP is ₹ 100 then CP = 85.4 $=\frac{85.4}{100}$ If SP is ₹ 1 then CP = **<u>85.4</u>** × 17.60 If SP is ₹ 17.60 then CP = 15.0304CP of the Mixture per kg = ₹ 15.0304 2nd difference = Profit by SP 1 kg of 2nd kind @ ₹ 15.0304 = 15.54 - 15.0304

= 0.50961st difference = ₹ 15.0304 - 13.84 = ₹ 1.1904 The Require Ratio = $(2^{nd} \text{ difference})$: $(1^{st} \text{ difference})$ = 0.5096 : 1.1904= 3:7[81] If $p^x = q$, $q^y = r$ and $r^2 = p^6$, then the value of xyz will be: (a) 0 (b) 1 (c) 3 (d) 6 (1 mark) Answer: $p^{x} = q, q^{y} = r \text{ and } r^{z} = p^{6}$ (d) If $q = p^x$, $q^y = r$ and $r^z = p^6$ $(q^{y})^{z} = p^{6}$ $[(p^{x})^{y}]^{z} = p^{6}$ $p^{xyz} = p^{6} = xyz = 6$ [82] If log x = m + n and log y = m - n, then log $(10x/y^2)$ = (a) 3n – m + 1 (b) 3m – n + 1 (c) 3n + n + 1(d) 3m + n + 1 (1 mark) Answer: (a) Log x = m + n and log y = m - nThen log $\left(\frac{10x}{y^2}\right) = \log 10x - \log y^2$ $= \log 10 + \log x - 2 \log y$ $= 1 + \log x - 2 \log y$ = 1 + (m + n) - 2 (m - n)= 1 + m + n - 2m + 2n= 3n – m + 1 [83] If $15(2p^2 - q^2) = 7pq$, where p and q are positive, then p : q will be: (a) 5:6 (b) 5:7 (c) 3:5 (d) 8:3 (1 mark) Answer: (a) If $15(2p^2 - q^2) = 7pq$ $30p^2 - 15q^2 = 7pq$

3.45

 $30p^{2} - 7pq - 15q^{2} = 0$ $30p^{2} - 25pq + 18pq - 15q^{2} = 0$ 5p(6p - 5q) + 3q(6p - 5q) = 0 (6p - 5q) (5p + 3q) = 0If 6p - 5q = 0 and 5p + 3q = 0 $6p = 5q \ 5p = - 3q$ $\frac{\mathbf{P}}{\mathbf{q}} = \frac{\mathbf{5}}{\mathbf{6}} = p : q = 5 : 6 \frac{\mathbf{P}}{\mathbf{q}} = \frac{-\mathbf{3}}{\mathbf{5}}$ (not possible)

2015 - DECEMBER

[84] The ratio of third proportion of 12, 30 to the mean proportion of 9, 25 is:

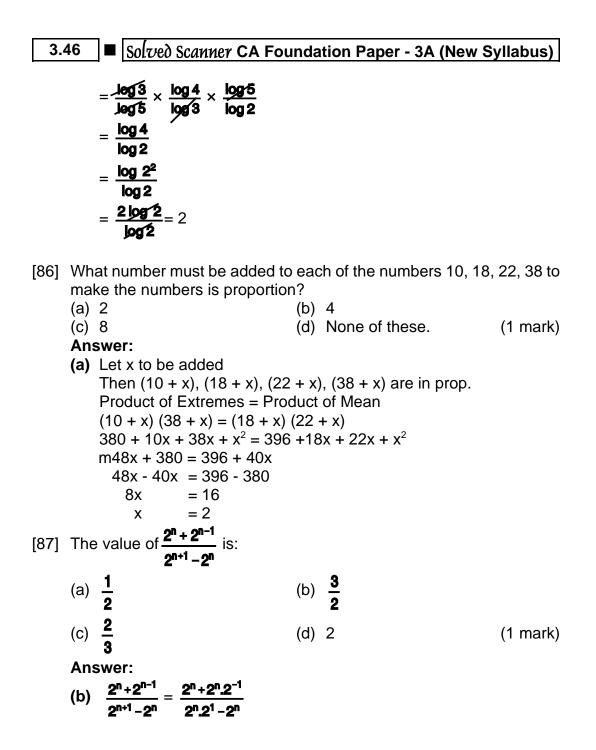
(a) 2:1	(b) 5:1
(c) 7:15	(d) 3:5

(1 mark)

Answer:

(b) The third proportion of 12,30 $c = \frac{b^2}{a} = \frac{(30)^2}{12} = \frac{900}{12} = 75$ The Mean proportion of 9,25 $b = \sqrt{ac} = \sqrt{9 \times 25} = \sqrt{225} = 15$ Ratio of third proportion of 12, 30 and Mean proportion of 9, 25 = 75:15 = 5:1[85] The value of $\log_5 3 \times \log_3 4 \times \log_2 5$. (a) 0 (b) 1 (c) 2 (d) $\frac{1}{2}$ (1 mark) Answer:

(c) $\log_5 3 \times \log_3 4 \times \log_2 5$



3.47

$$= \frac{2^{n}(1+2^{-1})}{2^{n}(2^{1}-1)}$$
$$= \frac{\left(\frac{1}{1}+\frac{1}{2}\right)}{(2-1)}$$
$$= \frac{\left(\frac{2+1}{2}\right)}{1}$$
$$= \left(\frac{3}{2}\right)$$

2016 - JUNE

- [88] The integral part of a logarithm is called ______ and the decimal part of a logarithm is called __ (b) Characteristic, Mantissa
 - (a) Mantissa, Characteristic (c) Whole, Decimal
- (d) None of these.

Answer:

(b) The integral part of a logarithms is called **Characteristic** and the decimal part of a logarithm is called mantissa.

[89] The value of
$$\begin{bmatrix} x^2 - (y - z)^2 \\ (x + z)^2 - y^2 \end{bmatrix} + \frac{y^2 - (x - z)^2}{(x + z)^2 - x^2} + \frac{z^2 - (x - y)^2}{(y + z)^2 - x^2} \end{bmatrix}$$
 is
(a) 0 (b) 1
(c) -1 (d) ∞ (1 mark)
Answer:
(b) $\frac{x^2 - (y - z)^2}{(x + z)^2 - y^2} + \frac{y^2 - (x - z)^2}{(x + y)^2 - z^2} + \frac{z^2 - (x - y)^2}{(y + z)^2 - x^2}$
 $= \frac{(x + y - z)(x - y + z)}{(x + z - y)} + \frac{(y + x - z)(y - x + z)}{(x + y + z)(x + y - z)} + \frac{(z + x - y)(z - x + y)}{(y + z + x)(y + z - x)}$
 $= \frac{x + y - z}{x + y + z} + \frac{y + z - x}{x + y + z} + \frac{z + x - y}{x + y + z}$

Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.48 $=\frac{\mathbf{X}+\mathbf{y}-\mathbf{Z}+\mathbf{y}+\mathbf{Z}-\mathbf{X}+\mathbf{Z}+\mathbf{X}-\mathbf{y}}{\mathbf{X}+\mathbf{y}+\mathbf{Z}}$ $=\frac{\mathbf{X}+\mathbf{y}+\mathbf{z}}{\mathbf{X}+\mathbf{y}+\mathbf{z}}=1$ [90] X, Y, Z together starts a business. If X invests 3 times as much as Y invests and Y invests two third of what Z invests, then the ratio of capitals of X, Y, Z is: (a) 3:9:2 (b) 6:3:2 (d) 6:2:3 (1 mark) (c) 3:6:2 Answer: (d) Given x = 3y and y = $\frac{2}{3}z$ $\frac{\mathbf{x}}{\mathbf{y}} = \frac{\mathbf{3}}{\mathbf{1}}$ and $\frac{\mathbf{y}}{\mathbf{z}} = \frac{\mathbf{2}}{\mathbf{3}}$ x : y = 3 : 1 and y : z = 2 : 3 $= 3 \times 2 : 1 \times 2$ = 6 : 2 x: y: z = 6: 2: 3[91] If log₄(x² + x) - log₄(x+1) = 2, then the value of X is: (a) 2 (b) 3 (c) 16 (d) 8 (1 mark) Answer: (c) If $\log_4 (x^2 + x) - \log_4 (x + 1) = 2$ $\log_4\left\{\frac{\mathbf{(x^2+x)}}{\mathbf{(x+1)}}\right\} = 2$ $\log_4\left\{\frac{\mathbf{x}(\mathbf{x}+\mathbf{1})}{(\mathbf{x}+\mathbf{1})}\right\} = 2$ $\log_4 x = 2$ $x = 4^{2}$ x = 16 [92] Value of $\frac{1}{\log_{3}^{60}} + \frac{1}{\log_{4}^{60}} + \frac{1}{\log_{5}^{60}}$ is :

[Chapter => 1] Ratio and Proportion, Indices...]
(a) 0 (b) 1 (c) 5 (d) 60 (1 mark)
Answer:
(b)
$$\frac{1}{\log_9 60} + \frac{1}{\log_4 60} + \frac{1}{\log_6 60}$$

 $= \log_{60} 3 + \log_{60} 4 + \log_{60} 5$ $\left[\frac{1}{\log_a b} = \log_b a \right]$
 $= \log_{60} (3 \times 4 \times 5)$
 $= \log_{60} 60$
 $= 1$
2016 - DECEMBER
[93] If $3^x = 5^y = 75^z$, then
(a) $x + y - z = 0$ (b) $\frac{2}{x} + \frac{1}{y} = \frac{1}{z}$ (1 mark)
Answer:
(c) $\frac{1}{x} + \frac{2}{y} = \frac{1}{z}$ (d) $\frac{2}{x} + \frac{1}{z} = \frac{1}{y}$ (1 mark)
Answer:
(c) If $3^x = 5^y = 75^z = k$ (let)
then $3^x = k, 5^y = k, 75^z = k$
 $3 = k^{1/x}, 5 = k^{1/y}, 75 = k^{1/z}$
we know that
 $75 = 3 \times 5 \times 5$
 $\frac{1}{x} = \frac{1}{x} + \frac{1}{y} + \frac{1}{y}$
on comparing
 $\frac{1}{z} = \frac{1}{x} + \frac{1}{y} + \frac{1}{y}$

Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.50 $\frac{1}{z} = \frac{1}{x} + \frac{2}{y}$ $\frac{1}{x} + \frac{2}{y} = \frac{1}{z}$ [94] If $\log 2 = 0.3010$ and $\log 3 = 0.4771$, then the value of $\log 24$ is: (a) 1.0791 (b) 1.7323 (c) 1.3801 (d) 1.8301 (1 mark) Answer: (c) If $\log 2 = 0.3010$ and $\log 3 = 0.4771$ then $\log 24 = \log (2 \times 2 \times 2 \times 3)$ $= \log 2 + \log 2 + \log 2 + \log 3$ $= 3 \log 2 + \log 3$ $= 3 \times 0.3010 + 0.4771$ = 0.9030 + 0.4771= 1.3801[95] If abc = 2, then the value of $\frac{1}{1+a+2b^{-1}} + \frac{1}{1+\frac{1}{2}b+c^{-1}} + \frac{1}{1+c+a^{-1}}$ is: (a) 1 (b) 2 (d) <u>1</u> (c) 3 (1 mark) Answer: (a) If abc = 2 ab $=\frac{2}{c} = 2c^{-1}$ $a = \frac{2}{bc} = 2b^{-1}c^{-1}$ bc = $\frac{2}{a}$ = 2 a⁻¹ b = $\frac{2}{ca}$ = 2 c⁻¹a⁻¹ ca = $\frac{2}{b}$ = 2 b⁻¹ c = $\frac{2}{ab}$ = 2 a⁻¹b⁻¹ $\frac{1}{1+a+2b^{-1}} + \frac{1}{1+\frac{1}{2}b+c^{-1}} + \frac{1}{1+c+a^{-1}}$ Given

3.51

$$= \frac{1}{1+a+2b^{-1}} + \frac{2b^{-1}}{2b^{-1}(1+\frac{1}{2}b+c^{-1})} + \frac{a}{a(1+c+a^{-1})}$$

$$= \frac{1}{(1+a+2b^{-1})} + \frac{2b^{-1}}{2b^{-1}+1+2b^{-1}c^{-1}} + \frac{a}{a+ac+1}$$

$$= \frac{1}{1+a+2b^{-1}} + \frac{2b^{-1}}{2b^{-1}+1+a} + \frac{a}{a+2b^{-1}+1}$$

$$= \frac{1+2b^{-1}+a}{1+a+2b^{-1}}$$

$$= 1$$

[96] There are total 23 coins of ₹ 1, ₹ 2 and ₹ 5 in a bag. If their value is ₹ 43 and the ratio of coins of ₹ 1 and ₹ 2 is 3:2. Then the number of coins of ₹ 1 is:

(a) 12 (b) 5 (c) 10 (d) 14 (1 mark) Answer: Total no. of coins = 23 (a) Ratio of ₹ 1 coin : ₹ 2 coins = 3 : 2 let No. of ₹ 1 coins = 3xNo. of ₹ 2 coins = 2xNo. of ₹ 5 coins = 23 - 3x - 2x= 23 - 5xTotal value of all coins = 43 $3x \times 1 + 2x \times 2 + (23 - 5x) = 43$ 3x + 4x + 115 - 25x = 43-18x = 43 - 115-18x = -72 $x = \frac{-72}{-18} = 4$ No. of $\gtrless 1 \text{ coins} = 3x = 3 \times 4 = 12$

3.52 ■ Solved Scanner CA Foundation Paper - 3A (New Syllabus)

2017 - JUNE

		nd c : d = 6 : 7, then a : d is:		
· · ·	24 : 35 I6 : 35	(b) 8:15 (d) 7:15	(1 mark)	
(C) Ansv		(d) 7.13	(T mark)	
(C) a	a : b = 2:3 $\frac{a}{b} = \frac{2}{3}$	(i)		
t	$c: c = 4:5$ $\frac{b}{c} = \frac{4}{5}$	(ii)		
C	$c: d = 6: 7$ $\frac{c}{d} = \frac{6}{7}$	(iii)		
Multiply equation (i) & (ii) & (iii)				
	$\frac{\mathbf{a}}{\mathbf{b}} \times \frac{\mathbf{b}}{\mathbf{c}} \times \frac{\mathbf{c}}{\mathbf{d}} = \frac{2}{3} \times \frac{4}{5} \times \frac{\mathbf{c}}{\mathbf{c}}$			
[98] The	value of log $(1^3 + 2^3 + 3^3)$	+ n^3) is equal to:		
· · ·	3 log 1 + 3 log 2 + +	•		
• •	$2 \log n + 2 \log (n+1) - 2$	-		
(c) (d) 1	og n + log (n+1) + log (2 I	n+1) – log 6	(1 mark)	
Ansv				
	$og (1^3 + 2^3 + 3^3 + \dots +$	n ³)		
	$= \log(n^3)$,		
	= log [<u>n(n+1)</u> ² 2			
=	= 2 log [<u>n(n+1)</u>]			
	= 2 [log n + log (n + 1) - l	• •		
	= 2 log n + 2 log (n + 1) -	0		
[99] If a =	√6 + √5 and b = √6 - √5 the √6 - √5	en the value of $\frac{1}{a^2} + \frac{1}{b^2}$ is equal	to:	
(a) 48	30	(b) 482		
(c) 48	34	(d) 486	(1 mark)	

Answer:

(b) If
$$a = \frac{\sqrt{6} + \sqrt{5}}{\sqrt{6} - \sqrt{5}}$$
 and $b = \frac{\sqrt{6} - \sqrt{5}}{\sqrt{6} + \sqrt{5}}$
 $a + b = \frac{\sqrt{6} + \sqrt{5}}{\sqrt{6} - \sqrt{5}} + \frac{\sqrt{6} - \sqrt{5}}{\sqrt{6} + \sqrt{5}}$
 $= \frac{(\sqrt{6} + \sqrt{5})^2 + (\sqrt{6} - \sqrt{5})^2}{(\sqrt{6} - \sqrt{5})(\sqrt{6} + \sqrt{5})}$
 $= \frac{6 + 5 + 2\sqrt{30} + 6 + 5 - 2\sqrt{30}}{(\sqrt{6})^2 - (\sqrt{5})^2}$
 $= \frac{22}{6 - 5} = \frac{22}{1} = 22$
 $a \cdot b = \left(\frac{\sqrt{6} + \sqrt{5}}{\sqrt{6} - \sqrt{5}}\right) \left(\frac{\sqrt{6} - \sqrt{5}}{\sqrt{6} + \sqrt{5}}\right) = 1$
 $\frac{1}{a^2} + \frac{1}{b^2} = \frac{b^2 + a^2}{a^2 b^2} = \frac{(a + b)^2 - 2ab}{(ab)^2}$
 $= \frac{(22)^2 - 2 \times 1}{(1)^2} = \frac{484 - 2}{1} = 482$

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2017 - DECEMBER

[100] The ratio of the number of ₹ 5 coins and ₹ 10 coins is 8 : 15. If the value of ₹ 5 coins is ₹ 360, then the number of ₹ 10 coins will be:

(a) 72	(b) 120	
(c) 135	(d) 185	(1 mark)

Answer:

(c) Ratio of ₹ 5 coins and ₹ 10 coins = 8 : 15

Let the No. of ₹ 5 coins = 8xand the No. of ₹ 10 coins = 15x

The value of ₹ 5 coins = ₹ 5 × 8x 360 = 40x

 $=\frac{360}{40}$ Х = 9 Х No. of ₹ 10 coins = 15x = 15 × 9 = 135[101] If $\log_3 [\log_4 (\log_2 x)] = 0$, then the value of 'x' will be: (a) 4 (b) 8 (c) 16 (d) 32 (1 mark) Answer: (c) If $\log_3 [\log_4 (\log_2 x)] = 0$ $\log_4 (\log_2 x) = 3^{\overline{0}}$ $\begin{bmatrix} \log_a b = x & b = a^x \end{bmatrix}$ $\log_4 (\log_2 x) = 1$ $\log_2 x = 4^1$ $\log_2 x = 4$ $x = 2^4$ x = 16 [102] If $\log\left(\frac{x-y}{2}\right) = \frac{1}{2}(\log x + \log y)$, then the value of $x^2 + y^2 =$ _____ (a) 2xy (b) 4xy (c) $2x^2y^2$ (d) 6xy (1 mark) Answer: (d) If $\log\left(\frac{x-y}{2}\right) = \frac{1}{2}(\log x + \log y)$ $2\log\left(\frac{\mathbf{x}-\mathbf{y}}{2}\right) = \log x + \log y$ $\log\left(\frac{\mathbf{x}-\mathbf{y}}{\mathbf{2}}\right)^{\mathbf{2}} = \log(\mathbf{x}\mathbf{y})$ $\left(\frac{\mathbf{x}-\mathbf{y}}{\mathbf{2}}\right)^{\mathbf{2}} = X\mathbf{y}$ $\left(\frac{\mathbf{x}-\mathbf{y}}{\mathbf{4}}\right)^{\mathbf{2}} = X\mathbf{y}$ $x^{2} + y^{2} - 2xy = 4xy$ $x^{2} + y^{2} = 4xy + 2xy$ $x^{2} + y^{2} = 6xy$

3.55

[103] If $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{5}$ and $\frac{1}{x}$ are in proportion, then the value of 'x' will be: (a) $\frac{15}{2}$ (b) $\frac{6}{5}$ (c) $\frac{10}{3}$ (d) $\frac{5}{6}$ (1 mark) Answer: (a) If $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{5}$, $\frac{1}{x}$ are in proportion then, product of extremes = Product of means $\frac{1}{2} \times \frac{1}{x} = \frac{1}{3} \times \frac{1}{5}$ $\frac{1}{2x} = \frac{1}{15}$ 2x = 15 x = 15/22018 - MAY

[104] If p : q is the sub-duplicate ratio of $p - x^2$: $q - x^2$, then x^2 is :

(a) $\frac{\mathbf{p}}{\mathbf{p} + \mathbf{q}}$ (b) $\frac{\mathbf{q}}{\mathbf{p} + \mathbf{q}}$ (c) $\frac{\mathbf{q}\mathbf{p}}{\mathbf{p} - \mathbf{q}}$ (d) None. (1 mark) Answer: (d) Sub duplicate ratio of $(\mathbf{p} - \mathbf{x}^2)$: $(\mathbf{q} - \mathbf{x}^2) = \sqrt{\mathbf{P} - \mathbf{x}^2}$: $\sqrt{\mathbf{q} - \mathbf{x}^2}$ $\mathbf{p}: \mathbf{q} = \sqrt{\mathbf{P} - \mathbf{x}^2} : \sqrt{\mathbf{q} - \mathbf{x}^2}$ $\frac{\mathbf{P}}{\mathbf{q}} = \frac{\sqrt{\mathbf{P} - \mathbf{x}^2}}{\sqrt{\mathbf{q} - \mathbf{x}^2}}$ an squaring both side $\frac{\mathbf{P}^2}{\mathbf{q}^2} = \frac{\mathbf{P} - \mathbf{x}^2}{\mathbf{q} - \mathbf{x}^2}$

■ Solved Scanner CA Foundation Paper - 3A (New Syllabus) 3.56 $p^2 (q - x^2) = q^2(p - x^2)$ $p^2q - p^2x^2 = q^2p - q^2x^2$ $p^2q - q^2p = p^2x^2 - q^2x^2$ pq (p - q) = (p^2+q^2)x^2 $pq (p - q) = (p+q)(p - q)x^{2}$ $x^{2} = \frac{pq(p-q)}{(p+q)(P-q)}$ $x^2 = \frac{\mathbf{pq}}{(\mathbf{p+q})}$ [105] The value of the expression : $a^{\log_{e}b \, \cdot \, \log_{b}^{o} \, \cdot \, \log_{b}^{d} \, \cdot \, \log_{d} t}$ (a) t (b) abcdt (c) (a + b + c + d + t)(d) None (1 mark) Answer: (a) $\mathbf{a}^{\log^b_a \cdot \log^o_b \cdot \log^d_d \cdot \log^t_d}$ $= a \frac{\log^{b}}{\log^{a}} \cdot \frac{\log^{c}}{\log^{b}} \cdot \frac{\log^{d}}{\log^{c}} \cdot \frac{\log^{f}}{\log^{d}}$ = a <u>log^t</u> log^a $= a \log_{a}^{t} [e^{\log_{a}} = x]$ = t [106] The mean proportional between 24 and 54 is: (a) 33 (b) 34 (c) 35 (d) 36 (1 mark) Answer: (d) Mean proportion $b = \sqrt{ac}$ $=\sqrt{24\times54}$ = **√1,296** = 36 [107] The value of $\log_4 9$. $\log_3 2$ is: (a) 3 (b) 2 (c) 9 (d) 1 (1 mark)

3.57

Answer:
(d)
$$\log_4 9. \log_3 2 = \frac{\log 9}{\log 4} \cdot \frac{\log 2}{\log 3}$$

 $= \frac{\log 3^2}{\log 2^2} \cdot \frac{\log 2}{\log 3}$
 $= \frac{2\log 3}{2\log 2} \cdot \frac{\log 2}{\log 3}$
 $= 1$
[108] $\frac{2^n + 2^n - 1}{2^{n+1} \square 2^n}$
(a) $\frac{1}{2}$ (b) $\frac{3}{2}$
(c) $\frac{2}{3}$ (d) $\frac{1}{3}$ (1 mark)
Answer:
(b) $\frac{2^n + 2^{n-1}}{2^{n+1} - 2^n} = \frac{2^n + 2^n \cdot 2^{-1}}{2^n \cdot 2^{-1} - 2^n}$
 $= \frac{2^n + (1 + 2^{-1})}{2^n \cdot (2^{-1})}$
 $= \frac{\left(1 + \frac{1}{2}\right)}{1}$
 $= \frac{\frac{3}{2}}{1}$